

SOLUTIONS FOR SEC 3 EXPRESS 2023 P1 V2

1		$\frac{2.7 + \sqrt{2.08}}{(-1.5)^4 - 0.02^2} = 0.82$ [2 SF] [B1]	
2		$35a^4 + 49\sqrt{a}$ $= \frac{5}{7}a^{\frac{2}{3}}$ [B1]	
3	a	$a - (3d + 4a) = a - 3d - 4a$ $= -3a - 3d$ [B1]	
	b	$8am - 12ak - 6dk + 4dm$ $= 8am - 12ak + 4dm - 6dk$ $= 4a(2m - 3k) + 2d(2m - 3k)$ [M1] $= 2(2a + d)(2m - k)$ [A1]	Presence of either one factorization correctly. Extracting common factor [M1] Erroneous working but able to get the final answer [M0A0]
	c	$\frac{2}{c^2 - 9} - \frac{5}{c + 3}$ $= \frac{2}{(c + 3)(c - 3)} - \frac{5}{c + 3}$ $= \frac{2}{(c + 3)(c - 3)} - \frac{5(c - 3)}{(c + 3)(c - 3)}$ [M1] $= \frac{2 - 5c + 15}{(c + 3)(c - 3)}$ $= \frac{17 - 5c}{(c + 3)(c - 3)}$ [A1]	making common denominator ($c^2 - 9$)($c + 3$) with all correct working on numerator [M1]
4	a	$\frac{1}{4}x - 8 \leq 3 - x < 9$ $\frac{1}{4}x - 8 \leq 3 - x$ or $3 - x < 9$ $\frac{5}{4}x \leq 11$ or $x > -6$ $x \leq 8\frac{4}{5}$ or $x > -6$ [either 1 is correct [M1]] Final: $-6 < x \leq 8\frac{4}{5}$ [A1]	

4	b	$\frac{2x + 7}{3} \leq b$ $x \leq \frac{3b - 7}{2}$ $\frac{3b - 7}{2} - 4$ $b - 5$ [B1] $a = -2.5$ [B1]	
5	a	$9.4 \times 10^{-11} \times 2 = 1.88 \times 10^{-10}$ [B1]	
	b	$1.06 \times 10^{-8} + 100 = 1.06 \times 10^{-10}$ [M1] Difference = 1.2×10^{-11} [A1]	
6	a	$396 = 2^2 \times 3^2 \times 11$ [B1]	Accept product but not in index form
	b	11 [B1]	
	c	$p = 2, q = 1$ [B1, B1]	
7	a	2 units rep 32 bars 1 unit rep 16 bars Connie has $16 \times 5 = 80$ [B1]	
	b	1 unit = 16 bars therefore $(5 - w) = 1$ [M1] $w = 4$ [A1]	Award M1 for presence of 64
8		$\frac{31}{50} \times 15 + \frac{63}{80} \times 15 + \frac{43}{50} \times 25 = 42.6125$ [M1] to score at least 75%, the remainder is 32.3875 [M1] $\frac{32.3875}{45} \times 100 = 71.9722$ Hence, she should score 72 marks [A1]	Attempt to find remainder [M1]
9	a	49 [B1]	
	b	12 [B1]	
	c	$n + n^2 + (4n - 1)$ [M1] $= n^2 + 5n - 1$ [A1]	Presence of n^2 or $(4n - 1)$ [M1]
10		Container A : Container B $\frac{25}{5} : \frac{10}{2}$ 125 : 8 [volume ratio] [M1] $\frac{125}{8}$ [M1] = 15.625 Number of containers B needed = 16 containers [A1]	Accept volume ratio 15625 : 1000 [M1]
11	a	Length = $\sqrt{(2 - 3)^2 + (3 - (-1))^2}$ [M1] $= 4.1231$ [A1] ≈ 4.12	

	b	$\text{gradient} = \frac{3 - (-1)}{2 - 3} = -4 \quad [\text{M1}]$ <p>Equation $y - 3 = -4(x - 2)$ $y = -4x + 11 \quad [\text{A1}]$</p>	
	c	$y = -4x + 11$ cuts the x axis: $y = 0$ $0 = -4x + 11$ $x = \frac{11}{4}$ coordinates = $(\frac{11}{4}, 0)$ [or equivalent] [B1]	
	d	$(0, 5)(0, -5)(5, 0)(5, -0)(\pm 3, 4)(\mp 3, 4)(3, \pm 4)(3, \mp 4)(-3, -4),$ $(\pm 4, 3), (\mp 4, 3), (4, \pm 3), (4, \mp 3), (-4, -3)$ [B1]	
12	a	$x^2 - 6x + 4$ $= (x - 3)^2 - 5 \quad [\text{B1}] \quad -5 \quad [\text{B1}]$	
	b	<p>Turning point = $(3, -5)$ Y intercept = 4</p> <p>[B1] for correct shape regardless of coordinates [B1] labelling the y intercept and turning point accurately</p>	
	c	$x = 3 \quad [\text{B1}]$	
13	a	$\angle APQ = \frac{(6 - 2) \times 180}{6} = 120 \quad [\text{B1}]$	
	b	$\angle SBC = 180 - 48 - 48 = 84$ $\angle ABC = 360 - 120 - 84 = 156 \quad [\text{M1}]$ $\frac{(n - 2) \times 180}{n} = 156 \quad [\text{M1}]$ or $n(180 - 156) = 360 \quad [\text{M1}]$ $180n - 360 = 156n$ $24n = 360$ $n = 15 \quad (\text{shown}) \quad [\text{A1}]$	Do not accept if candidates use 15 to show
14	a	$\frac{30}{10} = \frac{v}{8}$ $v = 24 \text{ m/s} \quad [\text{B1}]$	Or any appropriate method

	b	$\text{deceleration} = \frac{30 - 0}{30} = 1 \text{ m/s}^2 \quad [\text{B1}]$	
	c	$\text{Distance} = \frac{1}{2}(60 + 20)(30) = 1200 \quad [\text{M1}]$ $\text{Ave Speed} = \frac{1200}{60} = 20 \text{ m/s} \quad [\text{A1}]$	