

Topic: Surds and Polynomials

- 1 Given that $\left(\frac{\sqrt{40}}{3} - \frac{1}{\sqrt{10}}\right)\left(\frac{30}{\sqrt{5}}\right) = k\sqrt{2}$, find the integer value of k . [4]

- 2 Solve the following equations.
 - (i) $\sqrt{5x+2} - \sqrt{3x-8} = 0$ [2]
 - (ii) $\sqrt{7-6x} + x = -3x$ [3]

- 3 A rectangle has an area of $(8\sqrt{2} + 7\sqrt{5}) \text{ cm}^2$ and a length of $(3\sqrt{2} + \sqrt{5}) \text{ cm}$.
 Express in the form $a + b\sqrt{10}$, where a and b are integers,
 - (i) the breadth of the rectangle, [3]
 - (ii) the value of D^2 , where $D \text{ cm}$ is the length of the diagonal of the rectangle. [3]

- 4 If $5x^3 + Ax^2 + x + 3 = (x+1)(Bx^2 + Cx) + D$, find the values of A , B , C and D . [5]

- 5 Given that $f(x) = x^3 + 2x^2 - 17x + 6$,
 - (i) Show that $x - 3$ is a factor. [1]
 - (ii) solve the equation $f(x) = 0$, giving your answers to 2 decimal places where appropriate. [4]

- 6 The function f is defined by $f(x) = 2x^3 + ax^2 + bx - 12$.
 Given that $f(x)$ has a factor of $(x - 3)$ and leaves a remainder of -14 when divided by $(2x + 1)$,
 - (i) find the value of a and of b . [4]
 - (ii) find the remainder when $f(x)$ is divided by x . [1]

Answer Key

1	$k = 17$
2(i)	No solution. Cannot root negative number
2(ii)	$x = \frac{1}{2}$ (rej.) , $x = -\frac{7}{8}$
3(i)	$1 + \sqrt{10}$
3(ii)	$34 + 8\sqrt{10}$
4	$A = 6, B = 5, C = 1, D = 3$
5(ii)	$x = 3, -5.37, 0.37$
6(i)	$a = -5, b = 1$
6(ii)	Remainder = -12